Reconstruction of 2-D line radiation distributions in the JET MkIIGB Divertor using CCD camera tomography

A. Huber¹, P. Coad², D. Coster³, L.C. Ingesson⁴, G.F. Matthews², Ph. Mertens¹, V. Philipps¹, A. Pospieszczky¹, B. Schweer¹, G. Sergienko⁵, M. Stamp², K. Itami⁶ and contributors to the EFDA-JET workprogramme

¹Institut für Plasmafysik, Forschungszentrum Jülich GmbH, EURATOM Association, Trilateral Euregio Cluster, D-52425 Jülich, Germany, ²Euratom/UKAEA Fusion Association, Culham Science Centre, Abingdon, Oxon OX14 3DB,UK, ³Max-Planck-Institut für Plasmafysik, Garching, ⁴FOM-Instituut voor Plasmafysica, Nieuwegein, The Netherlands, ⁵Institute of High Temperatures, Russian Academy of Sciences, Moscow, Russian Federation, ⁶Japan Atomic Energy Research Institute, Naka-machi, Ibaraki-ken, Japan 311-0193

Introduction. The amount and spatial distribution of impurity radiation in the divertor of a tokamak is of fundamental importance for the behaviour of power exhaust, detachment, recombination, recycling and erosion/redeposition properties. Carbon impurity radiation in the divertor is indispensable to reduce the peak heat flux to the strike zones but carbon erosion also limits the lifetime of the target and leads to large tritium retention via co-deposition. In addition to line-integrated spectroscopic measurements, spatially resolved radiation of the various species obtained from tomographic inversion of 2D-CCD camera data is an important tool for diagnosing the role of impurity and hydrogen radiation in the divertor physics.

Experimental setup and principle of tomographic inversion. At JET, three CCD cameras (KL1 camera diagnostic, dynamical range of 8 bits, CCD-chip with 582x752 pixels) view the divertor in a nearly tangential geometry. They are coupled with interference filters and allow measurement of line-emission at three wavelengths (e.g. Dα, CII, CIII simultaneously). The images are recorded by three video recorder at a rate of 50 half frames per second. Concurrently, video signals are captured from cameras with a framegrabber board, which transfers images directly into the main memory.

The Fig.1a. displays the projections of lines of sight of the cameras into a poloidal plane showing only a reduced amount of chords (every 30 chord). There are enough chords in the whole divertor region to resolve the emission pattern along the radial direction with sufficient resolution but the resolution in z-direction (vertically) is limited due to the small number of chords crossing each other with large angle. Fig.1b. illustrates the lines of sight for eight locations selected in the divertor region, showing only the chords passing through these points. Since the range of angles between the lines of sight is smaller than 40 degrees, the resolution in the z-direction is limited.
The evaluation of the 2D-emission distribution in a poloidal plane assumes toroidal symmetry and is obtained by solving the matrix equation \( Ax = b \) using the Singular Value Decomposition method [1]. Here, \( A \) is the geometry matrix that contains the geometric information about the view of each CCD-pixel and the divertor structures limiting the corresponding lines of sight. The vector \( b \) contains the raw data (digitised CCD data), \( x \) is the solution. The Singular Value Decomposition (SVD) method decomposes the \( M \times N \) (\( M \) number of lines of sight, \( N \) number of divertor cells) matrix \( A \) into three matrixes \( A = U w V^T \), where \( U \) is an \( M \times N \) column orthogonal matrix, \( V^T \) is the transpose of an \( N \times N \) orthogonal matrix, and \( w \) is an \( N \times N \) diagonal matrix with nonnegative elements. The \( w \) matrix represents the singularity of the geometry matrix. When \( M > N \), the solution in the sense of minimising \( |Ax - b| \), is given by

\[
x = V 1/w U^T b
\]

where \( 1/w \) is the inverse of the \( N \times N \) diagonal matrix, for which, however, zero and small value elements are removed. The tolerance (\( TOL = w_{min} / w_{max} \)), defines the minimum \( w_i \) in \( 1/w \). To define the optimal tolerance, phantom studies have been performed using several test distributions as input. Fig.2a shows as an example a radiation profile of the form

\[
x_p(z, r) = \sum_{l=1,2} 1000.0 \times \exp((z/l)^2), \quad l = 7 cm
\]

aiming to simulate a toroidally elongated radiation source in the divertor region. Using the geometry matrix the virtual video image \( b^t \) can be easily calculated \( (b^t = Ax^p) \) and used as input for tomographic inversion. The result of this inversion with a optimised tolerance of 0.03 is shown in Fig.2b.

The optimised tolerance of 0.03 was found by choosing the minimum of the tomographical error \( \sigma_{\text{tomo}} = \{ \sum_i (x_i - x^p_i)^2 \}^{1/2} / \{ \sum_i (x^p_i)^2 \}^{1/2} = 0.5 \) and the smallest reconstruction error.
\[ \sigma_{rec} = \left\{ \sum (b_j - (Ax)_j)^2 \right\}^{1/2} / \left\{ \sum (b_j)^2 \right\}^{1/2} < 0.035 \] for our geometry. Due to the limited resolution in z-direction, the 2D reconstructed emission in the z-direction is enlarged (= 5cm).

**Results and Discussion.** L-mode Experiments have been performed with \( B_T = 2.4 \text{T} \) and \( I_p = 2 \text{MA} \) at an averaged central electron density of \( n_e = 3 \times 10^{19} \text{m}^{-3} \) and with additional NBI power of 1.85MW. The divertor strike points are moved along the vertical targets and the fixed Langmuir probes at about constant plasma density. The Fig.3a shows the time evolution of inner strike point (ISP) location (z-coordinate) and the saturation currents of the probes 3, 4 and 5 shown in Fig.3b which are maximal when the inner strike point is located on the corresponding probe (59.18s on probe 5 and 59.32s on probe 4). Fig.4 shows the camera images of \( \text{D}_\alpha \) (a) and CIII-emissions (e) in the divertor together with the reconstructed images for \( \text{D}_\alpha \) (b) and CIII-emissions (f) and the 2D solutions of the \( \text{D}_\alpha \) (c) and CIII-emissions (g) at a time of \( t=59.18 \text{s} \). Fig 4d and (h) show the 2D solutions of \( \text{D}_\alpha \) and CIII-emissions at a time of \( t=59.32 \text{s} \), where the strike point is moved up. As can be seen, the spatial location of the strike point obtained by the tomographical reconstruction correlates well with probe measurements of the ion saturation current. Thus, under attached conditions, the maximum of the hydrogen radiation is located always near the target plates at the position of the strike zones (at \( t=59.18 \text{s} \) at location of probe 5 and \( t=59.32 \text{s} \) at probe 4) but with a strong in-out asymmetry showing about a factor 2-5 more hydrogen radiation at the inner divertor leg. The reconstructed video images from the \( \text{D}_\alpha \) and CIII-emissions have a reconstruction error which is smaller than 0.04. As can be also seen, the CIII-radiation shows an opposite in-out asymmetry behaviour with the strongest CIII-emission located in the outer divertor leg. Strong CIII-radiation is also observed near the X-point for these L-mode attached plasma conditions.

The reconstructed \( \text{D}_\alpha \)-emission profiles have been compared with the line integrated emission of \( \text{D}_\alpha \)-hydrogen line radiation measured vertically from the top of the machine by an absolutely calibrated CCD camera array. As can be seen in Fig.5, the reconstructed poloidal
The $D_\alpha$-emission profiles match the data from the camera array very well. It should be also mentioned, that the comparison between SVD (presented here) and Non-Negativity Constraint (used for radiation tomography) [2,3] is in good agreement.

**Summary and conclusion.** 2D emission profiles of CIII and $D_\alpha$ radiation in the JET Divertor have been reconstructed by the Singular Value Decomposition method to obtain the emission pattern in a poloidal plane. In this contribution, L-mode conditions with the strike points moved along the vertical target plates have been analysed. The spatial location of the strike points obtained by tomographical reconstruction correlates well with the ion saturation current of the fixed target Langmuir probes. Under the attached conditions investigated, the maximum of the hydrogen radiation is located near the target plates at the position of the strike zone but with significantly more radiation from the inner leg compared with to the outer. The CIII-radiation is much stronger in the outer divertor with a strong contribution near the X-point. A good agreement between the emission pattern obtained from the different diagnostics is obtained. Also, the comparison between SVD and Non-Negativity Constraint Method shows good correlation.

[3] L.C. Ingesson et al., this conference